

Graph the piecewise-defined function. Then determine the left and right limits at the indicated values. Also determine if the function is continuous at the indicated value(s). If not, state why.

1.  $f(x) = \begin{cases} x^2, & x \leq 1 \\ x, & x > 1 \end{cases}$

Is  $f$  continuous at  $x = 1$ ?

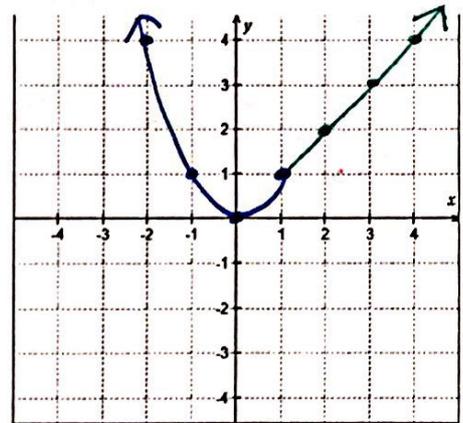
Why or why not? **yes**

$\lim_{x \rightarrow 1} f(x) = f(1)$

A)  $\lim_{x \rightarrow 1^-} f(x) = 1$

B)  $\lim_{x \rightarrow 1^+} f(x) = 1$

C)  $\lim_{x \rightarrow 1} f(x) = 1$



2.  $f(x) = \begin{cases} \sqrt{x+1}, & x > -1 \\ -x-2, & x \leq -1 \end{cases}$

Is  $f$  continuous at  $x = -1$ ?

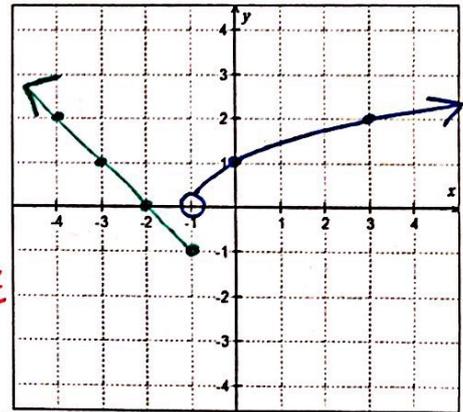
Why or why not? **no**

$\lim_{x \rightarrow -1} f(x) \neq f(-1)$

A)  $\lim_{x \rightarrow -1^-} f(x) = -1$

B)  $\lim_{x \rightarrow -1^+} f(x) = 0$

C)  $\lim_{x \rightarrow -1} f(x) = \text{DNE}$



3.  $f(x) = \begin{cases} x^3 + 1, & x \leq 0 \\ e^x, & x > 0 \end{cases}$

Is  $f$  continuous at  $x = 0$ ?

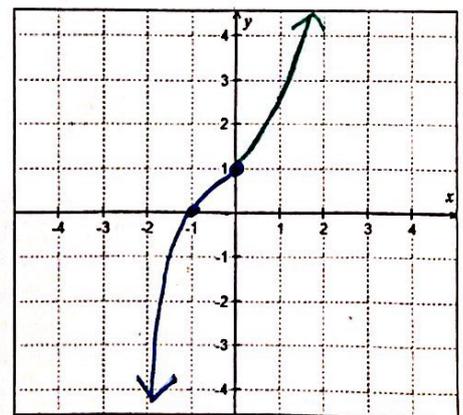
Why or why not? **yes**

$\lim_{x \rightarrow 0} f(x) = f(0)$

A)  $\lim_{x \rightarrow 0^-} f(x) = 1$

B)  $\lim_{x \rightarrow 0^+} f(x) = 1$

C)  $\lim_{x \rightarrow 0} f(x) = 1$



4.  $f(x) = \begin{cases} |x + 2|, & x \leq 1 \\ (x - 2)^2, & x > 1 \end{cases}$

Is  $f$  continuous at  $x = 1$ ?

Why or why not?

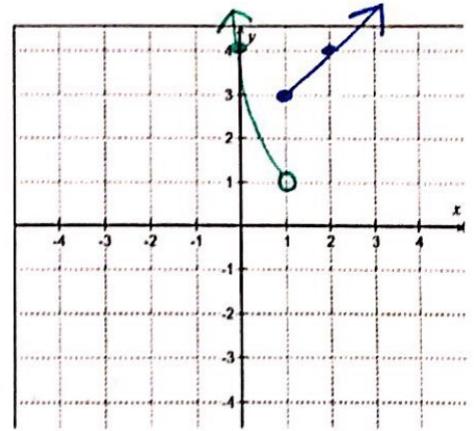
no

$\lim_{x \rightarrow 1} f(x) \neq f(1)$

A)  $\lim_{x \rightarrow 1^-} f(x) = 1$

B)  $\lim_{x \rightarrow 1^+} f(x) = 3$

C)  $\lim_{x \rightarrow 1} f(x) = \text{DNE}$



5.  $f(x) = \begin{cases} \sin x, & x > \frac{\pi}{2} \\ 3 - x^2, & x \leq \frac{\pi}{2} \end{cases}$

Is  $f$  continuous at  $x = \frac{\pi}{2}$ ?

Why or why not?

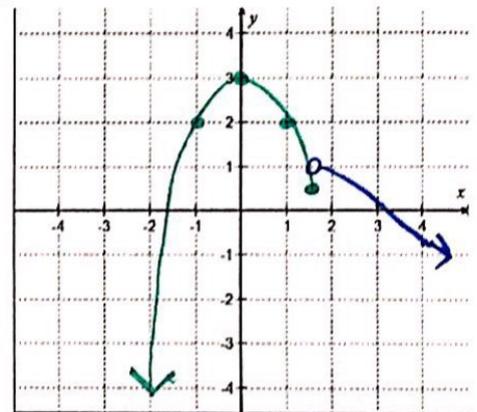
no

$\lim_{x \rightarrow \frac{\pi}{2}} f(x) \neq f(\frac{\pi}{2})$

A)  $\lim_{x \rightarrow \frac{\pi}{2}^-} f(x) = 0.53$

B)  $\lim_{x \rightarrow \frac{\pi}{2}^+} f(x) = 1$

C)  $\lim_{x \rightarrow \frac{\pi}{2}} f(x) = \text{DNE}$



6.  $f(x) = \begin{cases} 3 - x^2, & x \leq 1 \\ 2, & 1 < x < 3 \\ 5 - x, & x \geq 3 \end{cases}$

Is  $f$  continuous at  $x = 1$ ?

Why or why not?

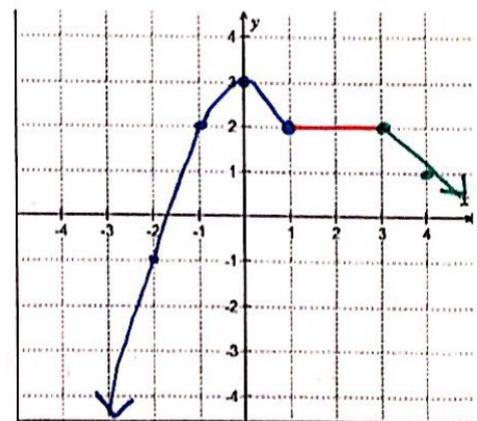
yes

$f(1) = \lim_{x \rightarrow 1} f(x)$

A)  $\lim_{x \rightarrow 1^-} f(x) = 2$

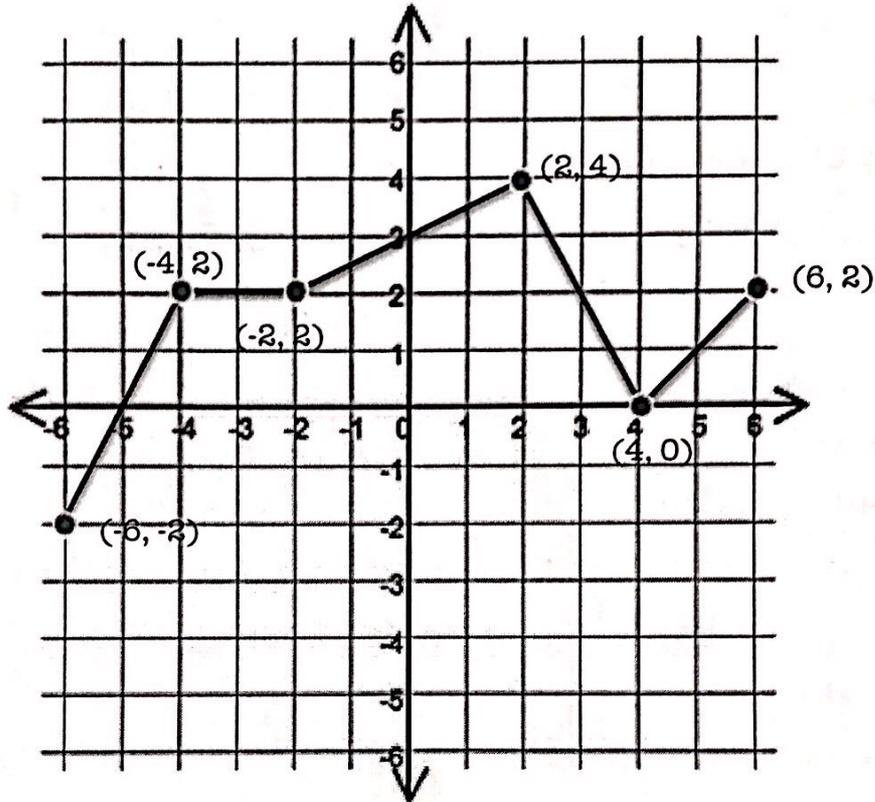
B)  $\lim_{x \rightarrow 1^+} f(x) = 2$

C)  $\lim_{x \rightarrow 1} f(x) = 2$



## Analyzing a Graph Worksheet #1

This is the graph of  $f(x)$ . Answer the questions below the graph.



1. What is $f(2)$ ?	4	2. What is $f(-5)$ ?	0
3. Where does $f(x) = 3$ ?	$x = 0 \text{ \& } 2.5$	4. At what $x$ value does this function have its maximum value?	2
5. At what $x$ value does this function have its minimum value?	-6	6. Over what $x$ values is this function increasing?	$(-6, -4) \cup (-2, 2) \cup (4, 6)$
7. Over what $x$ values is this function constant?	$[-4, 2]$	8. Over what $x$ values is this function positive?	$(-5, 6)$
9. Where does this function equal zero?	$x = -5 \text{ \& } 4$	10. Over what $x$ -values is this function negative?	$(-6, -5)$

GIVEN:  

$$f(x) = \frac{x^2 + 2x - 8}{x^2 - x - 2}$$

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

PERSON #1: Factor the function

$$y = \frac{(x+4)(x-2)}{(x-2)(x+1)}$$

PERSON #2: Check and initial: \_\_\_\_\_

PERSON #2: Find the x-intercept

$$y = \frac{x+4}{x+1}$$

$x+4=0$   
 $x=-4$

$(-4, 0)$

PERSON #3: Check and initial: \_\_\_\_\_

PERSON #3: Find the y-intercept

$$y = \frac{0+4}{0+1} = 4$$

$(0, 4)$

PERSON #4: Check and initial: \_\_\_\_\_

PERSON #4: Find the horizontal asymptote

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$$\frac{1}{1} = 1$$

$y=1$

PERSON #1: Check and initial: \_\_\_\_\_

PERSON #1: Find the vertical asymptote

$$x+1=0$$

$x=-1$

PERSON #3: Check and initial: \_\_\_\_\_

Person #2: Find the coordinates of the hole.

$$f(2) = \frac{2+4}{2+1} = \frac{6}{3} = 2$$

$(2, 2)$

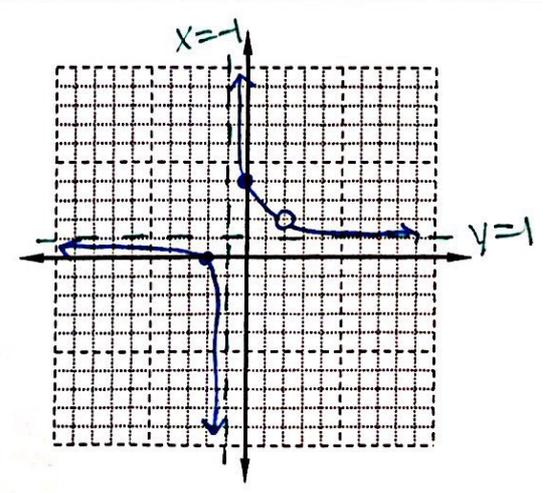
PERSON #4: Check and initial: \_\_\_\_\_

PERSON #3: Graph the asymptotes.

PERSON #4: Graph the function.

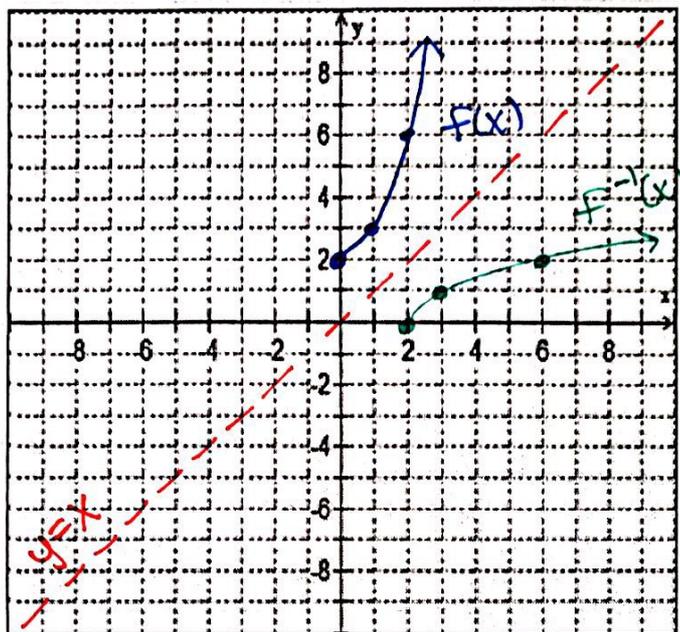
PERSON #1: Label the x-intercept.

PERSON #2: Label the y-intercept.



**Graph**

$$f(x) = x^2 + 2; x \geq 0$$



**Numerically**

$$f(x) = x^2 + 2; x \geq 0$$

$x$	$f(x)$
0	2
1	3
2	6
3	11
4	18
5	27
6	38

$x$	$f^{-1}(x)$
2	0
3	1
6	2
11	3
18	4
27	5
38	6

**Algebraic**

Find the inverse algebraically.

$$y = x^2 + 2 \quad x \geq 0$$

$$x = y^2 + 2$$

$$x - 2 = y^2$$

$$y = \sqrt{x - 2}$$

$$f^{-1}(x) = \sqrt{x - 2}, \quad x \geq 2$$

**Verbally**

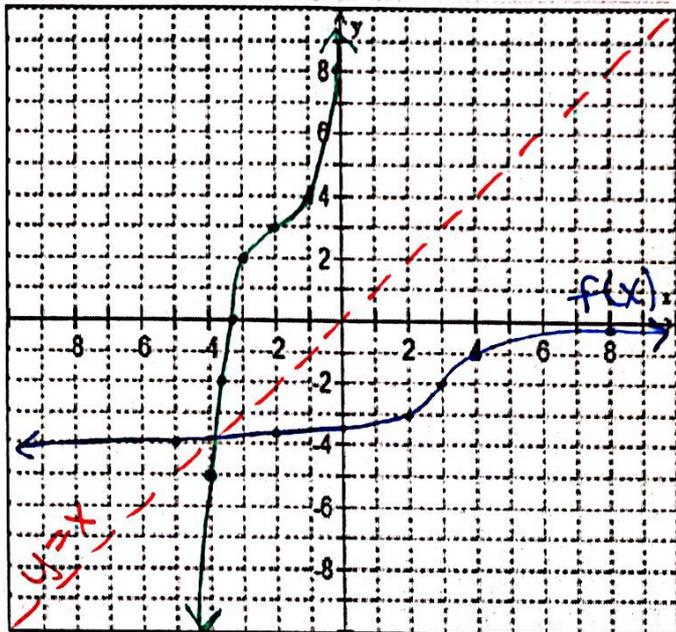
Use the table and the graph to answer the following:

$$f(x) = x^2 + 2; x \geq 0$$

	Function	Inverse
Domain:	$[0, \infty)$	$[2, \infty)$
Range:	$[2, \infty)$	$[0, \infty)$
x-intercept	none	(2, 0)
y-intercept	(0, 2)	none

**Graph**

$$f(x) = \sqrt[3]{x-3} - 2$$



**Numerically**

$$f(x) = \sqrt[3]{x-3} - 2$$

x	f(x)
-5	-4
-2	-3.7
0	-3.4
2	-3
3	-2
4	-1
8	-0.3

x	f <sup>-1</sup> (x)
-4	-5
-3.7	-2
-3.4	0
-3	2
-2	3
-1	4
-0.3	8

**Algebraic**

Find the inverse algebraically.

$$y = \sqrt[3]{x-3} - 2$$

$$x = \sqrt[3]{y-3} - 2$$

$$x+2 = \sqrt[3]{y-3}$$

$$(x+2)^3 = y-3$$

$$y = (x+2)^3 + 3$$

$$f^{-1}(x) = (x+2)^3 + 3$$

**Verbally**

Use the table and the graph to answer the following:

$$f(x) = \sqrt[3]{x-3} - 2$$

	Function	Inverse
Domain:	$(-\infty, \infty)$	$(-\infty, \infty)$
Range:	$(-\infty, \infty)$	$(-\infty, \infty)$
x-intercept	(11, 0)	(-3.4, 0)
y-intercept	(0, -3.4)	(0, 11)